

I claim:

1. A method of reconstructing images from data provided by at least one detector,  
comprising the steps of:

rotating a scanner in a single curve within a plane about a stationary object while  
5 scanning the object;  
scanning the object along a line transversal to the plane with the scanner; and  
reconstructing an exact image of the scanned object with a convolution based  
FBP(Filtered Back Projection) algorithm.

10 2. The method of claim 1, wherein the single curve includes the step of:  
rotating a C-arm device about a portion of the object.

3. The method of claim 1, wherein the single curve includes the step of:  
rotating a gantry about a portion of the object

15 4. The method of claim 1, wherein the single curve includes the step of:  
rotating between approximately 5 degrees up to approximately 360 degrees.

5. The method of claim 4, further comprising the step of:  
20 rotating over approximately 360 degrees about the object.

6. The method of claim 1, wherein the rotating and the subsequently scanning the  
object include the steps of:

moving a table supporting the object through a C-arm device and rotating the C-arm around the object.

7. The method of claim 1, wherein the step of reconstructing further includes the  
5 step of: shift invariant filtering of the cone beam projections; and  
back projection updating the image of the scanned object.
8. The method of claim 1, wherein the step of reconstructing includes the steps of:  
storing approximately 2 to approximately 4 cone beam (CB) projections in  
10 memory at a time; and  
using one family of lines for the step of reconstructing.
9. The method of claim 1, wherein the step of reconstructing includes the steps of:  
storing 1 cone beam (CB) projection in memory at a time; and  
15 using one family of lines for the step of reconstructing.
10. A method of reconstructing images from a planar curve scan and a line scan of an  
object, comprising the steps of:  
(a) collecting cone beam (CB) data from a detector during the planar curve scan  
20 and the line scan of the object;  
(b) identifying lines on a plane  $\Pi$  intersecting the cone beam, wherein the step (b)  
of identifying lines includes the steps of:  
(bi) if the x-ray source belongs to the line scan, project the planar curve  
scan onto  $\Pi$  and choose a discrete set of lines tangent to that projection;

(bii) if the x-ray source belongs to the planar curve scan, project the planar curve scan onto  $\Pi$  and choose a discrete set of lines parallel to that projection;

(c) preprocessing and shift invariant filtering said data along said lines, wherein  
5 the step (c) of preprocessing includes computing the derivative  $(\partial/\partial s)D_f(y(s), \Theta)$ , wherein

$s$  is parameter along the scan path, which determines point  $y(s)$  on the said path,

$D_f(y, \Theta)$  is the cone beam transform of  $f$  corresponding to the x-ray  
10 source located at the point  $y$  and the direction  $\Theta$ ,

$f$  is a function describing the object being scanned;

(d) back projecting said filtered data to form a precursor of said image; and

(e) repeating steps a, b, c, and d until an image of the object is reconstructed.

15 11. The method of claim 10, wherein shift-invariant filtering in step (c) includes convolving the derivative  $(\partial/\partial s)D_f(y(s), \Theta)$  with kernel  $1/\sin(\gamma)$  within a filtering plane containing  $y(s)$  and a line, identified in step (b) above, where  $\gamma$  is polar angle in the plane.

20 12. The method of claim 10, wherein the planar curve scan includes:  
a complete circle about the object.

13. The method of claim 10, wherein the planar curve scan includes:

less than complete circle about the object.

14. The method of claim 10, wherein the back-projection step (d) includes the steps of:

5 (di) fix a reconstruction point  $x$ , which represents a point inside the object being scanned, to reconstruct the image;

(dii) If  $s$  belongs to  $I(x)$ , then the said filtered CB data affects the image at  $x$  and one performs Steps (diii) to (dvii). If  $s$  is not inside the interval  $I(x)$ , then the said filtered CB data is not used for the image reconstruction at  $x$  and go back to

10 step (di) and choose another reconstruction point, here

$I(x)$  is the parametric interval corresponding to the section of the scan path bounded by the PI-line of  $x$ ;

PI-line of  $x$  is the line segment containing  $x$ , one endpoint of which belongs to the planar curve scan, and the other endpoint of which belongs to the line scan;

15 (diii) find the projection  $\hat{x}$  of  $x$  onto a detector plane  $DP(s)$  and unit vector  $\beta(s, x)$ , which points from  $y(s)$  towards  $x$ ;

(div) estimate a value of  $\Phi(s, \beta(s, x))$ , where  $\Phi(s, \beta(s, x))$  is the filtered CB data corresponding to the source position located at the point  $y(s)$  and direction  $\beta(s, x)$ ;

20 (dv) determine contribution from filtered CB data to the image being reconstructed at the point  $x$  by multiplying  $\Phi(s, \beta(s, x))$  by a weighting factor;

(dvi) add the said contribution to the image being reconstructed at the point  $x$  according to a pre-selected scheme; and  
(dvii) go to step (di) and choose a different reconstruction point  $x$ .

5 15. The method of claim 10, further comprising the steps of:

storing approximately 2 to approximately 4 cone beam (CB) projections in memory at a time; and

using one family of lines for each x-ray source position for the step of filtering.

10 16. A method of computing images derived from a planar curve scan and a line scan, comprising the steps of:

(a) collecting cone beam (CB) data from a detector during a planar curve scan and line scan of an object;

(b) identifying lines on a plane  $\Pi$  intersecting the cone beam, wherein the step (b)

15 of identifying lines includes the steps of:

(bi) if the x-ray source belongs to the line portion of the scan, project the planar curve portion of the scan onto  $\Pi$  and choose a set of lines tangent to that projection;

(bii) if the x-ray source belongs to the planar curve portion of the scan,  
20 project the planar curve portion of the scan onto  $\Pi$  and choose a set of lines parallel to that projection;

(c) preprocessing and shift invariant filtering said data along said lines, wherein the step (c) of preprocessing includes computing the derivative of  $D_f(y(s), \Theta)$

with respect to  $\Theta$  along a direction non-parallel to the plane determined by  $y(s)$  and a filtering line, the said plane being a filtering plane, here

$s$  is parameter along the scan path, which determines point  $y(s)$  on the said path,

5  $D_f(y, \Theta)$  is the cone beam transform of  $f$  corresponding to the x-ray source located at the point  $y$  and the direction  $\Theta$ ,

$f$  is a function describing the object being scanned;

(d) back projecting said filtered data to form a precursor of said image; and

(e) repeating steps a, b, c, and d until an image of the object is reconstructed.

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17. The method of claim 16, wherein shift-invariant filtering in step (c) includes convolving the data  $D_f(y(s), \Theta)$  with kernel  $1/\sin(\gamma)$  within a filtering plane, where  $\gamma$  is polar angle in the plane.

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18. The method of claim 16, wherein shift-invariant filtering in step (c) includes convolving the data  $D_f(y(s), \Theta)$  with kernel  $\frac{\partial}{\partial \gamma} \frac{1}{\sin(\gamma)}$  within a filtering plane, where  $\gamma$  is polar angle in the plane.

19. The method of claim 16, wherein shift-invariant filtering in step (c) includes  
20 convolving the derivative of  $D_f(y(s), \Theta)$  with a kernel within a filtering plane, the derivative of  $D_f(y(s), \Theta)$  is the derivative with respect to  $\Theta$  along a direction non-parallel to the filtering plane.

20. The method of claim 19, wherein  $y(s)$  belongs to the line portion of the scan.

21. The method of claim 19, wherein  $y(s)$  belongs to the planar curve portion of the  
5 scan.

22. The method of claim 16, wherein the planar curve scan includes:  
a complete circle about the object.

10 23. The method of claim 16, wherein the planar curve scan includes:  
less than complete circle about the object.

24. The method of claim 16, wherein the back-projection step (d) includes the steps  
of:

15 (di) fix a reconstruction point  $x$ , which represents a point inside the object being  
scanned, to reconstruct the image;

(dii) If  $s$  belongs to  $I(x)$ , then the said filtered CB data affects the image at  $x$  and  
one performs Steps (diii) to (dvii). If  $s$  is not inside the interval  $I(x)$ , then the  
said filtered CB data is not used for the image reconstruction at  $x$  and go back to

20 step (di) and choose another reconstruction point, wherein

$I(x)$  the parametric interval corresponding to the section of the scan path  
bounded by the PI-line of  $x$ ;

PI-line of  $x$  is the line segment containing  $x$ , one endpoint of which belongs to the planar curve scan, and the other endpoint of which belongs to the line scan;

(diii) find the projection  $\hat{x}$  of  $x$  onto a detector plane  $DP(s)$  and unit vector  $\beta(s, x)$ , which points from  $y(s)$  towards  $x$ ;

(div) estimate a value of  $\Phi(s, \beta(s, x))$ , where  $\Phi(s, \beta(s, x))$  is the filtered CB data corresponding to the source position located at the point  $y(s)$  and direction  $\beta(s, x)$ ;

(dv) determine contribution from filtered CB data to the image being reconstructed at the point  $x$  by multiplying  $\Phi(s, \beta(s, x))$  by a weighting factor;

(dvi) add the said contribution to the image being reconstructed at the point  $x$  according to a pre-selected scheme; and

(dvii) go to step (di) and choose a different reconstruction point  $x$ .

25. The method of claim 16, further comprising the steps of:

storing 1 cone beam(CB) projection in memory at a time; and

using one family of lines for each x-ray source position for the step of filtering.

26. A method of reconstructing images from data provided by at least one detector, comprising the steps of:

scanning the object with a planar curved scan and a line scan by at least one detector; and



reconstructing an exact image of the scanned object with a convolution based  
FBP(Filtered Back Projection) algorithm.

27. The method of claim 26, wherein the scanning step includes the step of:  
5 scanning by the planar curved scan before the line scan.
28. The method of claim 26, wherein the scanning step includes the step of:  
scanning by the line scan before the planar curved scan.
- 10 29. The method of claim 26, further comprising the step of:  
providing a C-arm device for the scanning of the object.
30. The method of claim 26, further comprising the step of:  
providing a gantry for the scanning of the object.
- 15 31. The method of claim 26, wherein the planar curve scan includes:  
at least a full circle scan about the object.
32. The method of claim 26, wherein the planar curve scan includes:  
20 less than a full circle scan about the object.
- ~~32.~~<sup>33</sup> The method of claim 26, further comprising the step of:  
consecutively scanning the object with another planar curve scan and another line scan.